

## [The algebra of Ratio]

The majority of conversions preserve ratio. For example, 1 inch is equal to 2.54 cm, 2 inches is equal to  $2 \times 2.54 = 5.08$  cm and the ratio is the same. Expressed using fractions notation:

$$1/2.54 = 2/5.08$$

If we want to know how many inches or how many cm a length is, we can write an equation with an unknown. For example, if we want to know how many cm there are in 12 inches

$$1/2.54 = 12/x$$

and now we can solve for x

$$x \cdot 1/2.54 = 12$$

$$x = 12 \times 2.54 = \dots$$

On the other hand if we want to know how many inches there are in 30 cm, we would have

$$1/2.54 = x/30$$

$$30 \times 1/2.54 = x = \dots$$

So the key is just keeping track of the ratio we're preserving. Of course, we can express the ratio in a different form too. In the example where we want to know how many cm there are in 12 inches, we can say that the ratio of inches,  $1/12$  will be the same as the ratio of cm  $2.54/x$ , and you'll note that the equation will rearrange equivalently to before.

$$1/12 = 2.54/x$$

$$x \cdot 1/12 = 2.54$$

$$x = 2.54 \times 12$$

How about some other conversions that preserve ratio?

1 Australian dollar is 0.7662 US dollars. How much in AUD is a book from the US that costs 35.99 USD?

$$1/0.7662 = x / 35.99$$

or

$$1/x = 0.7662 / 35.99$$

In fact if there's any kind of ratio relationship going on, we can set up this kind of equation.